

1- **Tick right (✓) or false (x) as appropriate (6 marks)**

- a) The  $Z|r(k-1) + u(k-1)| = R(z)$ ;  $r(k)$  unit ramp,  $u(k)$  unit step ( ) (3 marks)
- b)  $Z^{-1} \left| \frac{z^{-1}}{(a+z^{-1})} + \frac{a}{(a+z^{-1})} \right| = 2(-\frac{1}{a})^k$  ( ) (3 marks)

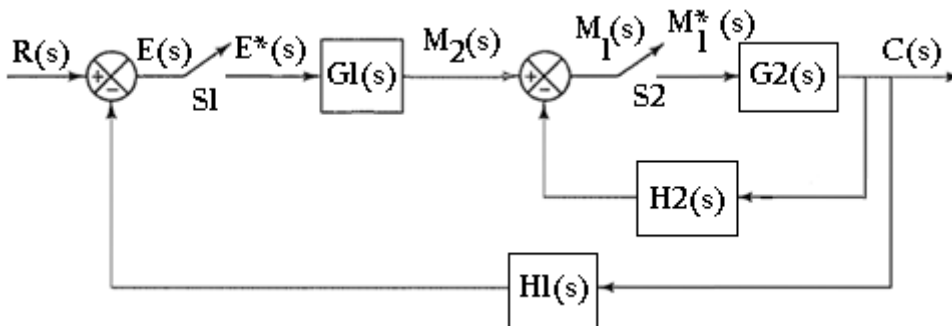
2- **Find the initial and final values of  $X(z)$  where (7 marks)**

$$X(z) = \frac{4z^4 - z}{(z^2 + 1 - z^{-2})(z^3 - 2z + z^{-1})}$$

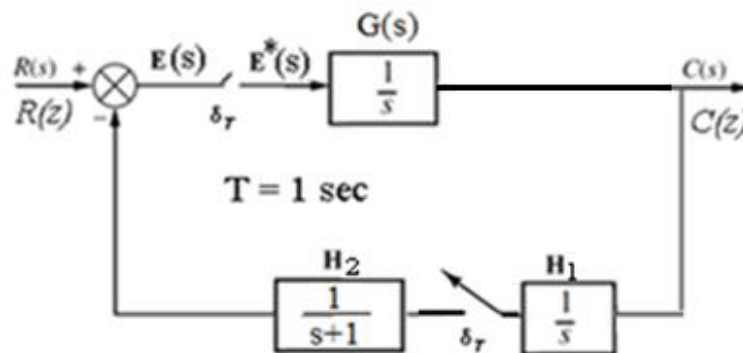
3- **Use the Convolution Integral Method to find the z transform of (7 marks)**

; Confirm your results using another method.  $X(s) = \frac{as+1}{(1-s^2)(a+s)}$

4- **Obtain the pulse transfer function of the system below: (8 marks)**



5- **For the discrete data system shown below: (12 marks)**



- Find the discrete time transfer function (6marks)
- Use the Jury test to determine the stability of the system when it is subjected to a Kronecker input; i.e.  $r(t) = \delta(k) = \text{Kronecker Delta}$ . (6 marks)

See underneath for some given useful information



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### Table of Laplace and Z-transforms

	$X(s)$	$x(t)$	$x(kT)$ or $x(k)$	$X(z)$
1.	–	–	Kronecker delta $\delta_0(k)$ 1 $k = 0$ 0 $k \neq 0$	1
2.	–	–	$\delta_0(n-k)$ 1 $n = k$ 0 $n \neq k$	$z^{-k}$
3.	$\frac{1}{s}$	$1(t)$	$1(k)$	$\frac{1}{1-z^{-1}}$
4.	$\frac{1}{s+a}$	$e^{-at}$	$e^{-akT}$	$\frac{1}{1-e^{-aT}z^{-1}}$
5.	$\frac{1}{s^2}$	$t$	$kT$	$\frac{Tz^{-1}}{(1-z^{-1})^2}$
6.	$\frac{1}{(s+a)^2}$	$te^{-at}$	$kTe^{-akT}$	$\frac{Te^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
7.	$\frac{s}{(s+a)^2}$	$(1-at)e^{-at}$	$(1-akT)e^{-akT}$	$\frac{1-(1+aT)e^{-aT}z^{-1}}{(1-e^{-aT}z^{-1})^2}$
8.	–	–	$a^k$	$\frac{1}{1-az^{-1}}$
9.	–	–	$a^{k-1}$ $k = 1, 2, 3, \dots$	$\frac{z^{-1}}{1-az^{-1}}$

The z transform is given as:

$$X(z) = \sum_{k=0}^{\infty} x(kT)z^{-k}$$

Initial value:  $x(0) = \lim_{z \rightarrow \infty} X(z)$

Final value theorem:  $x(\infty) = \lim_{z \rightarrow 1} [(1-z^{-1})X(z)]$

#### The convolution integral - simple poles

$$K_j = \lim_{s \rightarrow s_j} \left[ (s - s_j) \frac{X(s)z}{z - e^{Ts}} \right]$$

#### The convolution integral - repeated poles

$$K_i = \frac{1}{(n_i - 1)!} \lim_{s \rightarrow s_i} \frac{d^{n_i-1}}{ds^{n_i-1}} \left[ (s - s_i) \frac{X(s)z}{z - e^{Ts}} \right]$$